

## CLAIMS

We claim:

- 1 1. A method for adjusting an m-bit CRC of a sub-message, wherein the CRC  
2 generating polynomial is primitive or irreducible and the sub-message corresponds to  
3 a composite sub-message having n trailing zeroes, comprising:  
4 storing the m-bit CRC in an m-bit memory location;  
5 examining each bit of N, where N equals  $n \bmod (2^m - 1)$ , in order from the  
6 most significant bit to the least significant bit; the examining act for each examined  
7 bit comprising:  
8 finite field squaring the contents of the m-bit memory location, and;  
9 if the examined bit equals one, advancing the contents of the m-bit  
10 memory location to the next state as determined by the Galois field defined by the  
11 CRC generating polynomial.
- 1 2. The method of claim 1, wherein the CRC generating polynomial is a primitive  
2 polynomial.
- 1 3. The method of claim 1, wherein the CRC generating polynomial is an  
2 irreducible polynomial
- 1 4. The method of claim 1, wherein for each examined bit equaling one, the finite  
2 field squaring act and the advancing the contents act are performed simultaneously.

1 5. A method for adjusting an m-bit CRC of a sub-message, wherein the sub-  
 2 message corresponds to a composite sub-message having n trailing zeroes and the m-  
 3 bit CRC is equal or congruent to one, comprising:  
 4 storing the m-bit CRC in an m-bit memory location;  
 5 examining each bit of N, where N equals  $n \bmod (2^m - 1)$ , in order from the most  
 6 significant bit to the least significant bit; the examining act for each examined bit  
 7 comprising:  
 8 finite field squaring the contents of the m-bit memory location, and;  
 9 if the examined bit equals one, advancing the contents of the m-bit  
 10 memory location to the next state as determined by the Galois field defined by the  
 11 CRC generating polynomial.

1 6. The method of claim 5, wherein the CRC generating polynomial is neither  
 2 primitive nor irreducible.

1 7. A method for adjusting an m-bit CRC of a sub-message, the sub-message  
 2 corresponding to a composite sub-message having n trailing zeroes, wherein the CRC  
 3 generating polynomial is  $P(x)$ , comprising:

- 4 (a) computing  $Y = x^n \bmod P(x)$  using a lookup table;
- 5 (b) field multiplying the partial m-bit CRC and Y together; and
- 6 (c) field dividing the result from act (b) by  $P(x)$ , wherein the remainder forms  
 7 the adjusted partial m-bit CRC.

1 8. The method of claim 7, wherein act (a) comprises:

- 2 (d) factoring  $x^n$  into powers of two;

- 3 (e) computing the modulus  $P(x)$  of each factor from act (d) using a lookup
- 4 table, and
- 5 (f) computing  $Y$  by field multiplying together the results from act (e).

1 9. The method of claim 8, wherein  $P(x)$  represents a 32 bit number and the  
2 lookup table is no larger than 17 32-bit entries.

1 10. A method for adjusting an  $m$ -bit CRC of a sub-message, the sub-message  
2 corresponding to a composite sub-message having  $n$  trailing zeroes, wherein the CRC  
3 generating polynomial is  $P(x)$  and  $n$  is less than  $m$ , comprising:

- 4 (a) computing  $Y = x^n \bmod P(x)$  by setting  $Y = x^n$ ;
- 5 (b) field multiplying the partial  $m$ -bit CRC and  $Y$  together by shifting the
- 6 partial  $m$ -bit CRC to the left by  $n$  bits; and
- 7 (c) field dividing the result from act (b) by  $P(x)$ , wherein the remainder forms
- 8 the adjusted partial  $m$ -bit CRC.

1 11. A method of adjusting a CRC of a message composed of a plurality of sub-  
2 messages wherein the adjustment is in response to changes in a given sub-message,  
3 the given sub-message having a first  $m$ -bit CRC and corresponding to a first  
4 composite sub-message having  $n$  trailing zeroes, the changed sub-message having a  
5 second  $m$ -bit CRC and corresponding to a second composite sub-message having  $n$   
6 trailing zeroes, and wherein the CRC generating polynomial is primitive or  
7 irreducible, comprising:  
8 storing the first  $m$ -bit CRC in a first  $m$ -bit memory location;  
9 examining each bit of  $N$ , where  $N$  equals  $n \bmod (2^m - 1)$ , in order from the  
10 most significant bit to the least significant bit; the examining act for each examined

11 bit comprising:  
12                   finite field squaring the contents of the first m-bit memory location,  
13       and  
14                   if the examined bit equals one, advancing the contents of the first m-bit  
15       memory location to the next state as determined by the Galois field defined by the  
16       CRC generating polynomial, whereby the first m-bit memory location stores a third  
17       CRC of the first composite sub-message;  
18                   modulo 2 subtracting the third CRC from the CRC of the message to produce  
19       an intermediary CRC;  
20                   storing the second m-bit CRC in a first m-bit memory location;  
21                   examining each bit of N in order from the most significant bit to the least  
22       significant bit; the examining act for each examined bit comprising:  
23                   finite field squaring the contents of the second m-bit memory location,  
24       and;  
25                   if the examined bit equals one, advancing the contents of the second  
26       m-bit memory location to the next state as determined by the Galois field defined by  
27       the CRC generating polynomial, whereby the second m-bit memory location stores a  
28       fourth CRC of the second composite sub-message;  
29                   modulo 2 adding the fourth CRC to the intermediary CRC to produce the  
30       adjusted CRC of the message.

1    12.    The method of claim 11, wherein the first and second memory locations are  
2    the same.

1    13.    The method of claim 11, wherein the CRC generating polynomial is primitive.

1 14. The method of claim 11, wherein the CRC generating polynomial is  
2 irreducible.

1 15. A method of advancing an m-bit sequence through n states of a Galois field  
2 generated by a primitive or irreducible polynomial of degree m, comprising:  
3 storing the m-bit sequence in an m-bit memory location;  
4 examining each bit of N, where N equals  $n \bmod (2^m - 1)$ , in order from the  
5 most significant bit to the least significant bit; the examining act for each examined  
6 bit comprising:  
7 finite field squaring the contents of the m-bit memory location, and;  
8 if the examined bit equals one, advancing the contents of the m-bit memory location  
9 to the next state as determined by the Galois field.

1 16. The method of claim 15, wherein the polynomial is a primitive polynomial.

1 17. The method of claim 15, wherein the polynomial is an irreducible polynomial.